

## BACKGROUND

Plug-and-play Image Restoration (IR) has been widely recognized as a flexible and interpretable method for solving various inverse problems by utilizing any off-the-shelf denoiser as the implicit image prior. However, most existing methods focus on discriminative Gaussian denoisers. Although diffusion models have shown impressive performance for high-quality image synthesis, their potential to serve as a generative denoiser prior to the plug-and-play IR methods remains to be further explored.

## METHODS

In the previously published research by Zhang *et al.* [3], the Half-Quadratic-Splitting (HQS) algorithm is employed to iteratively tackle the Maximum A Posteriori (MAP) problem  $\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \frac{1}{2\sigma_n^2} \|\mathbf{y} - \mathcal{H}(\mathbf{x})\|^2 + \lambda \mathcal{P}(\mathbf{x})$  within the context of IR tasks. The algorithm's process can be stated mathematically as follows:

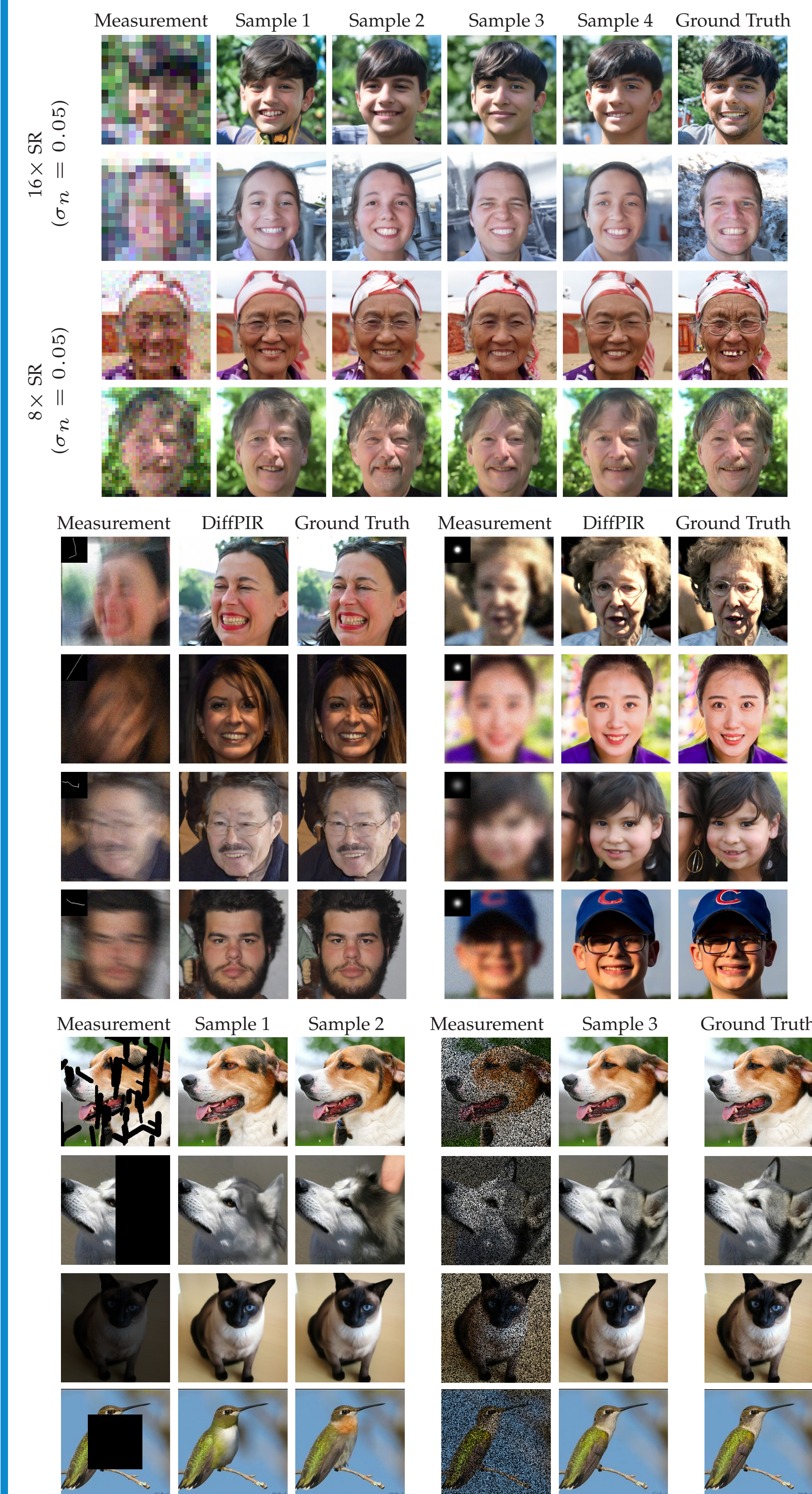
$$\begin{cases} \mathbf{z}_k = \arg \min_{\mathbf{z}} \frac{1}{2(\sqrt{\lambda}/\mu)^2} \|\mathbf{z} - \mathbf{x}_k\|^2 + \mathcal{P}(\mathbf{z}) \\ \mathbf{x}_{k-1} = \arg \min_{\mathbf{x}} \|\mathbf{y} - \mathcal{H}(\mathbf{x})\|^2 + \mu\sigma_n^2 \|\mathbf{x} - \mathbf{z}_k\|^2. \end{cases}$$

To harness the generative power of diffusion models, we adopt the diffusion sampling schedule, converting the original optimization methodology into a sampling technique. This introduces a novel plug-and-play sampling framework, defined as follows:

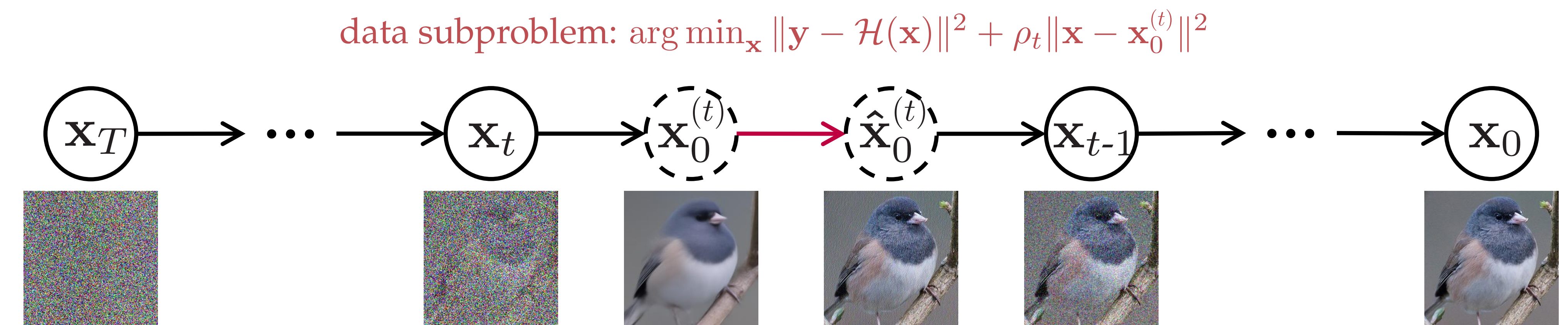
$$\begin{cases} \mathbf{x}_0^{(t)} = \arg \min_{\mathbf{z}} \frac{1}{2\bar{\sigma}_t^2} \|\mathbf{z} - \mathbf{x}_t\|^2 + \mathcal{P}(\mathbf{z}) \\ \hat{\mathbf{x}}_0^{(t)} = \arg \min_{\mathbf{x}} \|\mathbf{y} - \mathcal{H}(\mathbf{x})\|^2 + \rho_t \|\mathbf{x} - \mathbf{x}_0^{(t)}\|^2 \\ \mathbf{x}_{t-1} = \sqrt{\bar{\alpha}_{t-1}} \hat{\mathbf{x}}_0 + \sqrt{1 - \bar{\alpha}_{t-1}} (\sqrt{1 - \zeta} \hat{\epsilon} + \sqrt{\zeta} \epsilon_t) \end{cases}$$

Compared to the DDIM sampling framework, our method introduces an additional data subproblem. This extra component serves to guide the sampling process towards the posterior distribution  $p(\mathbf{x}|\mathbf{y})$ .

## QUALITATIVE RESULTS



## SAMPLING FRAMEWORK



**Illustration of our sampling method.** For every state  $\mathbf{x}_t$ , following the prediction of the estimated  $\mathbf{x}_0^{(t)}$  by the diffusion model, the measurement  $\mathbf{y}$  is incorporated by solving the data proximal subproblem (indicated by the red arrow). Subsequently, the next state  $\mathbf{x}_{t-1}$  is derived by adding *i.i.d* noise back and thus completing one step of reverse diffusion sampling.

## QUANTITATIVE RESULTS

FFHQ	$\sigma_n = 0.05$	Deblur (Gaussian)			Deblur (motion)			SR ( $\times 4$ )		
		Method	NFEs $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$
DiffPIR	100	27.36	<b>59.65</b>	<b>0.236</b>	<b>26.57</b>	<b>65.78</b>	<b>0.255</b>	26.64	<b>65.77</b>	0.260
DPS [1]	1000	25.46	65.57	0.247	23.31	73.31	0.289	25.77	67.01	<b>0.256</b>
DDRM [2]	20	25.93	101.89	0.298	-	-	-	27.92	89.43	0.265
DPIR [3]	>20	<b>27.79</b>	123.99	0.450	26.41	146.44	0.467	<b>28.03</b>	133.39	0.456

ImageNet	$\sigma_n = 0.05$	Deblur (Gaussian)			Deblur (motion)			SR ( $\times 4$ )		
		Method	NFEs $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$
DiffPIR	100	22.80	<b>93.36</b>	<b>0.355</b>	<b>24.01</b>	<b>124.63</b>	<b>0.366</b>	23.18	<b>106.32</b>	0.371
DPS [1]	1000	19.58	138.80	0.434	17.75	184.45	0.491	22.16	114.93	0.383
DDRM [2]	20	22.33	160.73	0.427	-	-	-	23.89	118.55	<b>0.358</b>
DPIR [3]	>20	<b>23.86</b>	189.92	0.476	23.60	210.31	0.489	<b>23.99</b>	204.83	0.475

FFHQ	$\sigma_n = 0.0$	Inpaint (box)		Inpaint (random)		Deblur (Gaussian)			Deblur (motion)			SR ( $\times 4$ )			
		Method	NFEs $\downarrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	PSNR $\uparrow$	FID $\downarrow$	LPIPS $\downarrow$	
DiffPIR	20	35.72	0.117	34.03	30.81	0.116	30.74	46.64	0.170	37.03	20.11	0.084	29.17	58.02	0.187
DiffPIR	100	<b>25.64</b>	<b>0.107</b>	<b>36.17</b>	<b>13.68</b>	<b>0.066</b>	<b>31.00</b>	<b>39.27</b>	<b>0.152</b>	37.53	<b>11.54</b>	<b>0.064</b>	29.52	<b>47.80</b>	<b>0.174</b>
DPS [1]	1000	43.49	0.145	34.65	33.14	0.105	27.31	51.23	0.192	26.73	58.63	0.222	27.64	59.06	0.209
DDRM [2]	20	37.05	0.119	31.83	56.60	0.164	28.40	67.99	0.238	-	-	-	30.09	68.59	0.188
DPIR [3]	>20	-	-	-	-	-	30.52	96.16	0.350	<b>38.39</b>	27.55	0.233	<b>30.41</b>	96.16	0.362

## REFERENCES

- [1] Hyungjin Chung and et al. Diffusion posterior sampling for general noisy inverse problems. *in ICLR, 2023.*
- [2] Bahjat Kawar and et al. Denoising diffusion restoration models. *in NeuIPS, 2022.*
- [3] Kai Zhang and et al. Plug-and-play image restoration with deep denoiser prior. *in IEEE PAMI, 2021.*

## MORE INFORMATION

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## DIFFUSION ART QR CODE

